

1 Title: Yield Prediction Through Integration of Genetic, Environment,
2 and Management Data Through Deep Learning

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51

52 Abstract

53 Accurate prediction of the phenotypic outcomes produced by different combinations of
54 genotypes, environments, and management interventions remains a key goal in biology with
55 direct applications to agriculture, research, and conservation. The past decades have seen an
56 expansion of new methods applied towards this goal. Here we predict maize yield using deep
57 neural networks, compare the efficacy of two model development methods, and contextualize
58 model performance using linear models, which are the conventional method for this task, and
59 machine learning models We examine the usefulness of incorporating interactions between
60 disparate data types. We find a deep learning model with interactions has the best average
61 performance. Optimizing submodules for each datatype improved model performance relative to
62 optimizing the whole model for all data types at once. Examining the effect of interactions in the
63 best performing model revealed that including interactions altered the model's sensitivity to
64 weather and management features, including a reduction of the importance scores for
65 timepoints expected to have limited physiological basis for influencing yield – those at the
66 extreme end of the season, nearly 200 days post planting. Based on these results, deep
67 learning provides a promising avenue for phenotypic prediction of complex traits in complex
68 environments and a potential mechanism to better understand the influence of environmental
69 and genetic factors.

70 71 Introduction

72 Prediction of an organism's phenotype is a key challenge for biology, especially when
73 integrating the effects of genetics, environmental factors, and human intervention. For many
74 traits, prediction is complicated by interactions between these factors. For example, within a
75 large multi-site, multi-genotype maize (*Zea mays*) study, more variation in grain yield is

76 explained by interactions between genetic and environmental factors than by genetic main
77 effects (Rogers *et al.* 2021). Including interaction effects between environmental and genomic
78 data can improve predictive accuracy in novel environments or for new cultivars (Li *et al.* 2021;
79 Jarquin *et al.* 2021).

80 Within agriculture, diverse methods have been applied to the task of predicting
81 phenotype ranging from classical statistics (Jarquin *et al.* 2021; Rogers *et al.* 2021; Rogers and
82 Holland 2021), machine learning (Westhues *et al.* 2021), physiological crop growth models
83 (Technow *et al.* 2015), to combinations of these and other methods (Messina *et al.* 2018;
84 Shahhosseini *et al.* 2021). Each model contains limitations such as lacking the capacity to
85 model complex non-linear responses (linear models) or interactions between factors,
86 interpretability within a biological framework (machine learning models), or dependence on
87 costly, low throughput data for calibration (crop growth models). Often simplifying assumptions
88 are introduced into the model (e.g. linearity), into the data (dimensionality reduction, feature
89 engineering), or into the experimental design (e.g. considering exclusively genetic,
90 environmental, or managerial effects to the exclusion of all others). While this approach creates
91 more manageable statistical models and enables a sufficiently powered study to be achieved
92 with fewer resources, it limits the capacity of a model to generalize to new genotypes,
93 environments, or management schemes. Furthermore, which factors are treated as “nuisance”
94 variables varies between communities within agriculture: geneticists often restrict management
95 regimes, while agronomists usually consider only a few cultivars. These approaches make it
96 difficult to investigate the interactions between genetic, environmental, and management
97 factors.

98 To predict an organism’s phenotype across genotypes, environments, and management
99 strategies simultaneously requires a dataset containing many combinations of these features.
100 Collecting such a dataset requires a large multi-site, multi-condition, experiment featuring

101 diverse genetic backgrounds. The Genomes to Fields Initiative (McFarland *et al.* 2020) seeks to
102 accomplish this aim. To date it has collected measurements of grain yield and other phenotypic
103 traits (plant height, days to silking, stalk lodging, and kernel row number, etc.) from about
104 180,000 plots planted at more than 160 environments. Environments are characterized using a
105 WatchDog 2700 Weather station (Spectrum Technologies, Inc.) which collects continuous
106 weather data throughout the season and collaborator submitted soil samples. Across the initiative,
107 over 2,500 maize hybrids have been tested, with Genotyping by Sequencing performed on
108 inbred parental lines used. Beyond the data collection, a means of effectively incorporating
109 diverse data types (genomics, management, soil measurements, weather, etc.) is needed,
110 particularly one that avoids simplifying assumptions where possible.

111 One method with the potential to accomplish this is that of deep neural networks (DNNs)
112 which have the capacity to approximate any function, provided they are sufficiently complex and
113 have sufficient examples to learn from. This capability is present regardless of whether they are
114 composed of dense fully connected (Hornik *et al.* 1989) or convolutional layers (Zhou 2020).
115 Additionally, DNNs “learn” directly from the data provided which enables reduced feature
116 engineering and dimensionality reduction. The methodology is also flexible with respect to data
117 type, allowing combination of variables that are static over a growing season (e.g. genotype)
118 and those that are dynamic (e.g. temperature) in a single model (Washburn *et al.* 2021). While
119 neural networks have been applied to the problem of predicting yield since at least 2001 (J. Liu
120 *et al.* 2001) this field is rapidly developing, with advances in theory, software, and hardware
121 enabling deeper and more accurate networks. Several recent studies have applied these
122 methods with a relatively large dataset either with (Washburn *et al.* 2021) or without (Khaki *et al.*
123 2020) a genetic component into the model, with little feature engineering performed. Both relied
124 instead on DNN’s capacity to learn useful data transformations from the data directly.

125

126 Despite their promise, DNNs are not a panacea for prediction. DNNs are prone to
127 overfitting to training data resulting in poor performance. Even when performing well, the
128 complexity of these models can obscure what aspects of the data the model is using. Advances
129 in deep learning have produced methods which reduce these limitations. For example, the use
130 of convolutional layers minimizes the potential of overfitting because they perform well with
131 fewer parameters relative to fully connected layers. Where fully connected layers are used,
132 overfitting can be reduced by randomly removing neurons from a layer with a certain “dropout”
133 percentage. While the inner workings of DNNs remain far less interpretable than simpler models
134 (e.g., Genomic BLUP or physiological models), methods have been developed to aid in
135 interpretation through identifying the importance of different features in the data which can be
136 applied. These methods include salience (Simonyan *et al.* 2014), guided backpropagation
137 (Khaki *et al.* 2020), and permutation based metrics (Shahhosseini *et al.* 2021) among others
138 (Samek *et al.* 2017). Here we use salience to illuminate the operation of the DNNs generated in
139 this study.

140 Here we, leverage DNNs’ capacity to determine feature importance from the data which
141 permits us to remain agnostic as to which features, or combinations of features are most
142 relevant. Furthermore, since DNNs are robust to lower--quality data and benefit from an
143 abundance of data, we employ a strategy of minimal feature transformation and curation and
144 maximal inclusion of observations. Using a minimally transformed dataset we begin the search
145 space considered in (Washburn *et al.* 2021), expand the space under consideration, and detail
146 a sequence of reproducible steps and objective heuristics which produced the models under
147 consideration. DNNs require an abundance of data for training. We begin by detailing a
148 workflow that incorporates a wider number of years from the Genomes to Fields Initiative in than
149 previous studies (Rogers *et al.* 2021; Washburn *et al.* 2021; Rogers and Holland 2021), while
150 also limiting the effect of errant and absent measurements. Improving on past studies, we

151 propose a new approach to model optimization whereby the model is broken into sub-modules
152 for each data type and interactions between them, then each submodule is consecutively
153 optimized, using a bayesian optimization procedure to find a suitable structure based on the
154 data itself. As far as we are aware, previous studies using deep learning for phenotypic
155 prediction have instead employed simultaneous optimization of all model components
156 (Washburn *et al.* 2021) or informal inductive tinkering. We compared models developed through
157 consecutive and simultaneous optimization and tested them against a variety of classic machine
158 learning and statistical methods to determine which performed best. To fairly assess model
159 performance we detail a strategy of constructing testing, training, and validation sets stratified
160 by season and location that is broadly useful to assessing model performance, while avoiding
161 overfitting the model to any location

162 Materials and Methods

163 Data Preparation

164 We used data from the Genomes to Fields (G2F) initiative for years 2014-2019
165 (McFarland *et al.* 2020), focusing on the sites within the continental United States. Each year's
166 data are publicly available (<https://www.genomes2fields.org/resources/>), including weather and
167 soil data for field sites, genomic data, management schedules (e.g., application of fertilizer,
168 herbicides, irrigation) and yield (in addition to other phenotypic variables). We augmented this
169 through additional genomic and weather data. Weather data retrieved from Daymet (Thornton *et al.*
170 2020) was used in quality control as discussed below and to infer data for locations which
171 lacked a functional weather station for some or all of the season. Daymet data was retrieved
172 through wget (Techtonik 2015).

173 These data are provided with some variability in format. Custom scripts were used to
174 aggregate and standardize terminology across years. Rather than itemizing each operation, we
175 restrict ourselves to those which are likely to be of interest to those working with similar data
176 sets. The scripts used are available through Bitbucket
177 (<https://bitbucket.org/washjake/maizemodel> and https://bitbucket.org/daniel_kick/maizemodel/).
178 Scripts were written in Python (Van Rossum and Drake 2009 p. 3) and rely on scientific and
179 common general libraries (Seabold and Perktold 2010; Pedregosa *et al.* 2011; *fuzzywuzzy*
180 2017; Virtanen *et al.* 2020; team 2020; Harris *et al.* 2020; Da Costa-Luis *et al.* 2022) along with
181 plotting libraries for exploratory visualizations (Hunter 2007 p. 200; Inc 2015; Waskom 2021;
182 Kibirige *et al.* 2021). We used Anaconda (“Anaconda Software Distribution” 2021) to manage
183 the virtual environment.

184 We reduced the dimensionality of the genomic data with principal components analysis
185 (PCA) before use. Provided genomes were loaded into TASSEL version 5.2.74 (Bradbury *et al.*
186 2007) and filtered. Filter parameters were intended to be relatively unrestrictive, while still
187 reducing the data enough for PCA to complete with the memory available. We arrived at these
188 filtering parameters through inductive tinkering (i.e., iteratively increasing filtering until the
189 dataset was sufficiently small for the process to not exhaust available memory). First, we
190 restricted the loci to those having a heterozygosity of at least 0.001. Next, we converted the
191 data to a numerical genotype, and imputed missing values are imputed with the mean. The
192 quality of observations varied through the dataset. We discarded samples if they had missing
193 values for 90% or more of loci. Once the data was reduced, the genomes were PCA
194 transformed. We find that 31% of the variance is explainable by the first 8 principal components
195 (PCs), 50% is explainable by the first 50 PCs, and >99% of the variance is explainable by 1725
196 PCs.

197 Each hybrid's coordinates in PC space were estimated as the average between its
198 parent's coordinates. This was done rather than creating simulated hybrids due to hardware and
199 software constraints. If simulated hybrids are generated in TASSEL the number of observations
200 input into PCA is substantially increased (i.e., all observed combinations of genomes are
201 transformed, not all observed genomes). Completion of PCA would thus requires stricter filtering
202 for the analysis to be completed. By estimating hybrid values after PCA transformation we retain
203 a greater number of loci per observation influencing the PCs.

204 Environmental data required preprocessing as well. The soil dataset contains many
205 missing values, having an average completion rate of 47% across all site-by-year combinations.
206 For each variable in the soil dataset, missing values were first linearly interpolated across years
207 with respect to location. Locations with no observations for any years were imputed using k-
208 nearest neighbors based on the nearest 5 neighbors for remaining missing values. Within the
209 reported weather data, we observed evidence of equipment malfunction and imputed or
210 adjusted values using linear models.

211 First, we removed outliers and extreme observations by limiting the data to those days
212 where the difference between the minimum daily value estimated by Daymet and the measured
213 value were in the central 60% of the distribution. This removes values from the G2F reported
214 weather data (based on more inexpensive and error prone equipment) that are inconsistent with
215 the Daymet data. Next, linear models were generated using the 4 Daymet estimated variables
216 with the strongest correlations with the target variable across the dataset. All combinations of
217 additive models containing 0-4 of these predictors plus an optional site-by-year term were fit and
218 ranked using Akaike information criterion corrected for small sample size (AICc). The best
219 performing model for each metric was used to impute missing weather data. In the case of
220 temperature measurements, which exhibited the most apparent evidence of instrumental error,

221 observed values were also replaced if the difference between the expected and observed value
222 was greater than 1.5x the interquartile range of those differences.

223 The representation of management data was refined. Fertilizer applications were
224 decomposed into the quantity of nitrogen, phosphorus, and potassium applied. Where fertilizer
225 applications were lacking an application date, we estimated the time difference relative to the
226 planting date with K-NN imputation ($k = 5$) to cluster based on application quantity. To define the
227 time window under consideration, we used the earliest within-season fertilizer application and
228 the day of the latest harvest to bound the weather and management data. This resulted in
229 selecting 75 days prior to planting, 1 planting day, and the 204 subsequent days (210 total
230 days).

231 Weather and management time-series data were clustered to reduce their
232 dimensionality for use in machine learning and linear models. For each variable we used time
233 series k-means with dynamic time warping implemented through the tslearn library (Tavenard *et*
234 *al.* 2020). K was optimized by calculating the silhouette score for k between 2 and 40 then
235 selecting the k one less than the lowest k in which the silhouette score decreased. Where
236 needed clusters were represented categorically through one hot encoding.

237 Defining Training, Validation, and Test sets

238 We generated train/test splits randomly, with the constraint that any location-year
239 combination could appear in only the testing or training set. Nearby experimental sites were
240 grouped for the purpose of generating training and testing sets. The method of generating splits
241 was: (1) one site group was selected at random and added to the testing set. (2) Each site-
242 group-by-year combination was down sampled so that it had no more observations than were
243 found in the smallest site-group-by-year combination in the testing set. This prevented
244 overrepresentation of any one group in the training data. (3) This process was repeated until the

245 testing set accounted for 10% to 15% of the total observations *and* at least 40,000 observations
246 remained across the training and test set. If these conditions were not met the process was
247 repeated with a different seed value.

248 During deep neural network hyperparameter selection, we limited overfitting to a single
249 validation set by using Monte Carlo cross-validation, stratified by site-group-by-year. Folds were
250 created while controlling for year by location groups by drawing the same number of site-group-
251 by-year groups as were present in the test set (3 for the test/train split used here) but without
252 further down sampling. The selected groups constituted the validation set. This was repeated 10
253 times and the membership of the folds preserved throughout training or hyperparameter search
254 for a single model. To enable reproducibility, random number generator seeds were used in
255 train/validate split searching and Monte Carlo cross-validation fold generation.

256 Prior to hyperparameter selection and training the input data was centered and scaled
257 based on the mean (~147.397 bushels per acre) and standard deviation (~48.169 bushels per
258 acre) of the yield in the training data, i.e., $y = \frac{y_{Original} - 147.397}{48.169}$. Transforming the data prior to
259 determining cross validation folds potentially introduces an information leak within the
260 hyperparameter selection process (i.e., the data used in evaluation, here across cross validation
261 folds, by influencing the mean and standard deviation used in centering and scaling the data).
262 However, this does not create an issue for final evaluation of the model's performance because
263 the test set data were not used in these calculations.

264 Model Preparation

265 Overview

266 We sought to model genotype by environment by management interaction effects (GEM
267 effects) in maize yield and to determine utility of doing so. To this end we optimized DNNs to
268 predict yield with a single data modality (i.e., only genomic data, soil characteristics, or time

269 series data each by itself). We use one dimensional convolutional layers to capture the time
270 dependent features of weather data, which have previously been used in yield prediction for this
271 task (Khaki *et al.* 2020; Washburn *et al.* 2021). We used dense, fully connected layers for the
272 other submodules of the DNN.

273 We pursued two strategies for tuning and training GEM models: Consecutive Optimization
274 (CO) and Simultaneous Optimization (SO). CO tunes the hyperparameters of networks predicting
275 yield from a single data modality (genomic data, soil data, or weather and management time
276 series data). Next, the prediction neurons are discarded and the output of the penultimate layer
277 of each single modality network enters a set of layers to permit interactions between data
278 modalities. Hyperparameters for the interaction layers are then tuned. The SO strategy by
279 contrast allows for all hyperparameters to be selected concurrently, both those which affect the
280 processing of a single data modality and those influencing interactions between modalities.

281 **Hyperparameter Search and Training**

282 We selected model architecture through a hyperparameter search using the
283 `BayesianOptimization` tuner provided within the `keras-tuner` package (O'Malley *et al.* 2019).
284 Models were written in Keras (Chollet and others 2015) with Tensorflow as a backend (Martín
285 Abadi *et al.* 2015) and run in a Singularity container (Kurtzer *et al.* 2017; SingularityCE
286 Developers 2021). The subnetworks processing exclusively genomic and exclusively soil data,
287 along with the interaction subnetwork, are constructed exclusively of dense (i.e., fully
288 connected) layers, each subject to batch normalization and dropout. The weather/management
289 processing subnetwork is composed of two one-dimensional convolution layers followed by
290 batch normalization and a pooling layer. The output of this subnetwork is flattened before
291 entering the interaction subnetwork. Hyperparameter ranges explored for each network are
292 listed in Table 1. To avoid overfitting to the validation data we used a custom subclassed
293 version of the tuner to randomly select one of the previously defined validation folds. This is

294 done rather than using mean loss over all folds to avoid increasing the computational cost 10-
295 fold while still preventing overfitting to a single validation set.

296 For all DNNs, a maximum of 40 hyperparameter sets were explored. In cases where no
297 convolution layers were being varied (CO models with only genomic, or only soil data, and the
298 interaction layers trained for the same strategy) hyperparameters were trained for a maximum of
299 1000 epochs with an early stopping patience of 7 epochs or more. For cases in which
300 convolution layers were varied (Sequential Optimization model with only weather and
301 management data, Concurrent Optimization model) hyperparameters were trained for a
302 maximum of 500 epochs with an early stopping patience of 5 epochs. This difference is due to
303 practical rather than theoretical reasons as the convolutional networks required notably more
304 time per epoch to fit. Regardless of network type, if the hyperparameters optimization had not
305 concluded by 290 hours after the script began, the process was terminated and the
306 hyperparameter sets completed by that point were considered.

307 To ensure the selected hyperparameter set performs well across validation sets, the top
308 4 hyperparameter sets for each model were trained for 1000 epochs and evaluated on all 10
309 defined testing/validation set splits. Next, the validation losses over the duration of training were
310 used to calculate the mean and standard deviation for each epoch. Then the training duration
311 was split into 10 bins and the average of the sum of validation loss mean and standard deviation
312 was calculated, i.e. $loss_{bin} = \frac{\sum_{i=1}^n \bar{l}_i + s_i}{n}$ where i is epoch relative to the beginning of the bin, \bar{l}_i is
313 the mean validation loss across cross validation folds at the i^{th} epoch and s_i is the standard
314 deviation of the same. The hyperparameter set with the lowest value for the most bins was used
315 going forward.

316 For the best hyperparameter set, we selected a training duration from the validation
317 losses. For each fold we calculated a rolling mean of validation loss with a window size of 20
318 epochs. Next, for each epoch we calculated the sum of the mean and standard deviation of the

319 rolling mean and the total rolling validation loss. Then we found the epochs which minimized
320 these two values (subtracting 10 from the epoch number to account for the window size). The
321 disagreement between the epochs which minimized these values ranged from 2 epochs in the
322 case of the CO Genomic model and CO interaction model up to 404 epochs for the CO weather
323 and management model. We decided to use total rolling validation loss to decide on the epoch
324 number for each model. This metric resulted in more training epochs for all models except the
325 SO model. Incorporating a more sophisticated method for selecting training duration is a
326 possible improvement for future studies. With the selected hyperparameters and training
327 duration we fit each model 10 times to account for random initialization and saved each
328 replicate and its training history.

329 Benchmarking Models

330 Overview

331 To contextualize the performance of the generated deep neural networks we use the
332 same training data to fit linear and classic machine learning models. These models often require
333 fewer resources and time to train than deep neural networks. For linear models we consider a
334 small collection of models that varied with respect to the independent variables present, whether
335 interactions are included, and whether effects are fixed or random. For supervised machine
336 learning models, we selected and optimized four methods: k-nearest neighbor (KNN), radius
337 neighbor regression (RNR), random forest (RF), and support vector regression with a linear
338 kernel (SVR).

339 Linear Models

340 To aid in evaluating the efficacy of the models produced, we constructed linear models
341 varying in the scope of included data and model complexity. The simplest model was an

342 intercept model, i.e., every predicted yield equals the mean yield in the training set. We
343 considered three models using the genomic data alone: fixed effects for PCs 1-8 (31% variance
344 explained), fixed effects for PCs 1-50 (50% variance explained), and random effects for the first
345 8 PCs. For soil data we considered two models, one with all factors as fixed effects and one
346 with all factors as random effects. From weather and management data we produced three
347 models, using all factors as fixed effects, using clusterings of the top five most salient features
348 (i.e., Water total, solar radiation mean, maximum temperature, mean wind direction, vapor
349 pressure) identified in the weather and management data (averaging over time points) as fixed
350 effects, and as random effects. Most salient features were taken from the deep neural network
351 with the lowest average test set RMSE (CO Interaction). All weather and management data
352 were represented as categorical clusters as described in “Data Preparation”.

353 We evaluated five models using a combination of data sources. In three fixed effect
354 models we incorporated: (1) PCs 1-8 and the five most salient weather features’ clusterings, (2)
355 the same plus all soil features, and (3): the effects in “1” plus interactions between each PC and
356 weather factor cluster. The two random-effects models we fit using PCs 1-8 and the selected
357 weather clusters excluding or allowing interactions. We fit Fixed effect models with the linear
358 model function in R (R Core Team 2021) and random effect models with lme4 (Bates *et al.*
359 2015). This analysis was aided by common data wrangling and convenience libraries (Wickham
360 *et al.* 2019; Bache and Wickham 2020; Müller 2020; Izrailev 2021) and feather file read/write
361 capabilities through arrow (Richardson *et al.* 2021).

362 Classical Machine Learning Models

363 Additional machine learning models were implemented through scikit-learn (Pedregosa
364 *et al.* 2011; Buitinck *et al.* 2013) and hyperparameters for each were optimized through the
365 hyperopt library (Bergstra *et al.* 2013) run within a Docker container. In a workflow similar to that
366 of the deep neural network models, we generated models for each data modality independently,

367 and with all data available. Time series data was represented as clusters as described in “Data
368 Preparation”. For each model we allowed the following hyperparameters to vary as described:
369 (1) K Nearest Neighbors (KNN): neighbors = 1-250, weights = 'uniform' or 'distance'; (2) Radius
370 Neighbors Regressor (RNR): radius = 0.01-2000, weights = 'uniform' or 'distance'; (3) Random
371 Forest (RF), maximum depth = 2-200, Minimum samples per leaf = 0-0.5; and (4) Support
372 vector machine with a linear kernel (SVR): Loss = 'epsilon_insensitive' or
373 'squared_epsilon_insensitive', C = 1-5 (log uniformly distributed).

374 Cross validation folds matching those as described previously and average loss across
375 all folds was measured. We tested a minimum of 115 combinations for each model and selected
376 the best performing hyperparameters for each input dataset, reported in Table 5. Following
377 selection, we trained each model and produced predictions on the testing and training data. This
378 was repeated 10 times to account for randomness in model fitting.

379 Model evaluation

380 For every model described above we calculate predicted yields for the test set and
381 calculate root mean squared error ($RMSE = \sqrt{\frac{\sum_i^n Prediction_i - Observation_i}{n}}$), normalized RMSE
382 percent ($nRMSE = 100\% * \frac{RMSE}{\left(\frac{\sum_i^n Observation_i}{n}\right)}$) and R^2 using SciPy (Virtanen *et al.* 2020).

383 Unless stated otherwise in the text RMSE and nRMSE will refer to the average value across
384 replicates. Two observations were not predictable using the fit radius neighbors regressor and
385 were predicted as the training set mean. For the best performing DNN we calculated and
386 visualized the salience of features for each data modality. To examine the influence of allowing
387 interactions we contrast these saliences with the saliences of SO single modality DNNs.
388 Saliences were calculated by Tf-keras-vis (Kubota 2021). Visualizations were created with the

389 use of rjson (Couture-Beil 2018), patchwork (Pedersen 2020), and ggplot2 (Wickham *et al.*
390 2019).

391 Data Availability Statement

392 Data for maize phenotypes, genotypes, field site soil properties and on location weather
393 recordings from the Genomes to Fields Initiative data (McFarland *et al.* 2020) is publicly
394 available through the CyVerse Discovery Environment. We used data from 2014 to 2019 which
395 correspond to the following DOIs: 2014 – 2017 (0.25739/frmv-wj25), 2018 (10.25739/anqq-
396 sg86), and 2019 (10.25739/t651-yy97). Additional genomic data was provided by Natalia de
397 Leon, Dayane Lima, and Cinta Romay worked with Joseph Gage through personal
398 communication. These data will be available through CyVerse. Following public release, a
399 version of these data containing all genomic data used in this study will be available through
400 Zenodo (10.5281/zenodo.6916775). At time of writing, this repository contains the eigenvectors
401 resulting from the principal components analysis are provided to enable transformation of
402 provided genomes. Additional weather measurements were retrieved from Daymet (Thornton *et*
403 *al.* 2020). Custom python scripts for downloading, aggregating and processing these data are
404 available on bitbucket (<https://bitbucket.org/washjake/maizemodel> and
405 https://bitbucket.org/daniel_kick/maizemodel/) in the notebooks directory (files with the prefix
406 0.0 to 0.5).
407

408 Results

409 Deep Neural Networks can--but do not necessarily--outperform 410 competing model types

411 When all data sources are incorporated, the CO DNN achieves the best (i.e., lowest)
412 average RMSE (when not otherwise specified, values refer to the average across replicates),
413 followed by a fixed effect model with interaction effects (nRMSE 14.6% vs 14.9%, RMSE 0.948
414 vs 0.959) (Figure 2, Table 6). Despite this, with 2/10 replicates of the CO DNN model
415 underperform this fixed effect model. Variability in DNN performance across replicates can be
416 caused by the random initialization of the weights at the start of training.

417 Following CO DNN and a linear model with interaction effects, an exclusively additive
418 linear model incorporating all data modalities ranked third (nRMSE 15.0%, RMSE 0.980) and
419 one excluding soil data ranked fourth (nRMSE 15.1%, RMSE 0.981). Random effects models
420 with and without soil data (nRMSE 15.2%, 15.3%, RMSE 0.991, 0.994) and SO DNN (nRMSE
421 15.7%, RMSE 1.024) followed. Of the machine learning models only support vector regression
422 with a linear kernel (SVR) and K Nearest Neighbor (KNN) outperformed a simple intercept
423 model. We find similar results for R^2 (Supplemental Figure 2, Table 6).

424 A DNN is not the best performing model when data is restricted to a single modality.
425 When restricted to genomic data, KNN, followed by linear models with fixed or random effects
426 are the only ones which outperform the intercept model (nRMSE 16.5%, 16.6%, 16.7%, 16.7%,
427 RMSE 1.078, 1.084, 1.085, and 1.088, KNN, linear fixed effects, linear random effects, intercept
428 model). SVR performed particularly poorly on this data (nRMSE 18.7%, RMSE 1.212) -- nRMSE
429 2% or RMSE of 0.131 above the intercept model. Incorporating only soil data SVR performed
430 best (nRMSE 16.3%, RMSE 1.059) with all other models being within nRMSE 0.261% or 0.017
431 RMSE of the intercept model. Most models performed better when instead trained on weather/

432 management data with the exception of the random forest (RF) which had an nRMSE 5.729%,
433 RMSE of 0.373 *above* the intercept model. SVR (nRMSE 15.1%, RMSE 0.985) and a fixed
434 effects model (nRMSE 15.2%, RMSE 0.993) performed remarkably well. CO DNN is capable of
435 outperforming these methods, but not uniformly. 2/10 replicates underperformed the intercept
436 model resulting in a nRMSE 15.6%, RMSE of 1.018 while the median values were nRMSE
437 15.2% and RMSE is 0.992.

438 **Consecutive Optimization resulted in a larger, more accurate final**
439 **network.**

440 Two hyperparameter selection strategies were employed, Consecutive Optimization
441 (CO) and Simultaneous Optimization (SO), have the same range of possible networks
442 (hyperparameter ranges are listed in Table 1), the same data driving network selection and both
443 use bayesian optimization. Despite this, the strategy applied resulted in notably different final
444 architectures. A visual summary of the relative differences between network hyperparameters is
445 shown in Figure 1, with the hyperparameter values listed in Tables 2 and 3. Supplementary
446 Figure 1 provides a visual overview of the network architecture. We consider the effect of CO vs
447 SO on each of the four subnetworks (processing exclusively genomic, soil, or
448 weather/management factors or interactions between data modalities), listed in decreasing
449 order of approximate similarity.

450 The output of this subnetwork is flattened before entering the interaction subnetwork
451 genomic subnetworks resulting from CO and SO are both two layers, but the CO model widens
452 somewhat (layer 1 = 83 units, 16% dropout, layer 2 = 133 units 23% dropout) while the SO
453 model begins over twice as wide and constricts more (layer 1 = 196 units, 15% dropout, layer 2
454 = 47 units 6% dropout). The interaction subnetworks contained a similar number of layers (CO:
455 5 vs SO: 6), but while CO resulted in layers with similar widths before constricting at the last

456 layer (units = 152, 207, 206, 188, 44, dropout percentages = 19%, 29%, 0.5%, 20%, 24%), SO
457 resulted in layers with very few units initially which are later expanded (units = 10, 25, 126, 204,
458 45, 134, dropout percentages = 10%, 15%, 2%, 16%, 24%, 19%). The soil subnetwork resulting
459 from CO is notably deeper than the one from SO (7 and 2 dense layers respectively) but also
460 narrows more by the last processing layer (2 vs 27 units). Finally, in the weather and
461 management subnetwork CO resulted in a notably deeper network (6 pairs vs 2 pairs of
462 convolution layers) but used a similar number of filters in the final convolution layer pairs (CO
463 294 vs SO 303).

464 The performance of these networks differs as well. The CO network was better at
465 predicting yield in the testing set. It achieved a lower mean RMSE (CO: 0.948 vs SO: 1.024)
466 and was more consistently accurate across replicates (standard deviation CO: 0.013 vs SO:
467 0.035). Similar results were seen in the normalized errors (nRMSE CO: 14.6% SO: 15.7%,
468 standard deviation CO: 0.197%, SO: 0.531%). Similarly, average R^2 was higher in the CO
469 network (CO: 0.171 vs SO: 0.032) and more consistent across replicates as well (standard
470 deviation CO: 0.022 vs SO: 0.065).

471 Model performance differences are due, in part, to the heuristic used to select the
472 number of training epochs and different tendencies for these models to overfit. The heuristic
473 used to select the number of training epochs (sum of the rolling validation loss) and alternate
474 heuristic considered (mean plus standard deviation of the rolling validation loss) resulted in
475 networks with comparable performance, having on average 0.001 less RMSE. With the
476 exception of the SO DNN, this also resulted in longer training durations. These ranged from an
477 additional 2 epochs in the cases of the CO genomic and interaction models and as many as 404
478 epochs in the case of the CO weather/management, as shown in Table 4.

479 These training durations were often considerably longer than the optimal values as seen
480 in Figure 1B. Furthermore, the length of overtraining appears loosely proportional to the present

481 minimum average RMSE each model achieved. The SO and CO weather models had the
482 largest differences between optimal and used epoch numbers – differences of 697 and 563
483 epochs respectively and achieved 121% and 110% of the minimum possible RMSE. The CO
484 soil model trained an excess 185 epochs but only had RMSE at 102% minimum. The two
485 training durations closest to the optimum were the CO genomic model (2 epochs over) and the
486 SO model (77 epochs over). These models performed at just 100.2% and 101% minimum.

487 The SO model overfits faster and to a greater extent than the full CO model, which does
488 not show evidence of substantial overfitting (Figure 1B d, e). The SO model achieves a loss
489 lower than the CO model, and the accuracy worsens rapidly with further training. The different
490 network sizes (CO containing more layers) may account for this difference. Improved heuristics
491 for training duration could represent an opportunity for future refinements, which these results
492 suggest could both increase goodness of fit and reduce the computational resources needed to
493 train these models.

494

495 Model performance generally improves through incorporating 496 multimodal data and interactions

497 Incorporating multiple data sources and allowing interactions between data types
498 generally appears to improve accuracy. Within the tested DNNs, allowing interactions increased
499 performance relative to single modality models. The potential exception to this is the SO DNN
500 (nRMSE 15.7%, RMSEs 1.024) and the CO weather/management model (nRMSE 15.6%,
501 RMSE 1.018). Despite this, the former's distribution had lower dispersion with a standard
502 deviation of RMSEs 0.035 relative to 0.074. Within the linear models tested, allowing
503 interactions increased accuracy in the fixed effect model by 0.3% nRMSE or 0.023 RMSE but
504 *decreased accuracy* in random effects models by 0.04% nRMSE or 0.003 RMSE.

505 In purely additive linear models, incorporating additional data modalities decreases error.
506 The largest difference in fixed effect models is for genomic data (improvement of 1.916%
507 nRMSE, 0.125 RMSE), followed by soil data (improvement of 1.722% nRMSE, 0.112 RMSE),
508 and weather/management data (improvement of 0.531% nRMSE, 0.035 RMSE). The same
509 trend is seen in models with random effects models, albeit with less variation in improvements
510 (improvements of 1.436% nRMSE, 0.094 RMSE genomic, 1.349% nRMSE, 0.089 RMSE soil,
511 1.132% nRMSE, 0.074 RMSE weather/management).

512 This pattern does not hold for the machine learning methods tested. For KNN, the model
513 trained on exclusively weather data performed best (0.218% nRMSE, 0.014 RMSE better than
514 using all data) although using all data sources did improve accuracy relative to only genomic or
515 soil data. SVR follows a similar pattern but is more exaggerated with using exclusively weather
516 data resulting in an improvement of 0.862% nRMSE or 0.059 RMSE relative to all data whereas
517 all data represented an improvement relative to genomic and soil data. Random forests did not
518 follow this trend– Genomic and soil models performed better than all data by 0.026% and
519 0.375% or 0.002 and 0.024 RMSE respectively, whereas the weather and management model
520 performed 5.439% nRMSE or 0.354 RMSE worse. Finally, radius neighbor regression (RNR)
521 performance was worst using only genomic data (1.112% nRMSE, 0.072 RMSE worse than all
522 data) but using only soil or only weather data improves model accuracy by 0.185% and 0.090%
523 nRMSE or 0.012 and 0.006 RMSE respectively.

524 Which factors are most important to the CO DNN?

525 Among the genomic data we observe no major trend in salience with respect to PC
526 (Supplementary Figure 3 A.). The two most salient PCs are PC 26 (0.423) and PC 24 (0.402)
527 which account for 0.350% and 0.392% of the total genomic variance respectively. Given that
528 these saliences are relative to principal components, using salience to implicate specific genes

529 or gene loci is infeasible. Among the soil factors we find that the five with the highest average
530 salience were soil pH (0.488), phosphorus ppm (0.487), potassium ppm (0.485), sulfate ppm
531 (0.436), and percent organic matter (0.413) (Supplementary Figure 3 C).

532 Within the weather and management data, considering the average salience across the
533 season (Supplementary Figure 3 D) five factors achieved an average salience greater than
534 0.140 – Total water (0.245), average solar radiation (0.198), maximum temperature (0.175),
535 average wind direction (0.174), and estimated vapor pressure (0.173). The majority of factors
536 had an average salience between 0.140 and 0.10 with six falling below this threshold – average
537 soil temperature (0.095), maximum wind speed (0.084), average soil moisture (0.076),
538 phosphorus applied (0.052) and potassium applied (0.033). Additionally, we find specific time
539 points which appear to be salient broadly with the most salient region of time is within the first
540 few days of planting, indeed 8 of the 10 days with the highest average salience are days 2-9
541 following planting.

542 How is factor importance altered by inclusion of interactions?

543 The full CO model, in addition to performing best (albeit by a small margin), presents an
544 opportunity to directly compare the influence of interactions between data modalities on the
545 salience of factors because the single modality subnetworks are identical except for the
546 prediction layer. The salience of genomic factors differs notably between the two networks
547 (Supplementary Figure 3 B). Salience of PCs differs by as much as 0.432 (PC 24), with the
548 difference in salience of the first 8 PCs (31% variance explained) ranging from 0.200 (PC1) to
549 0.309 (PC7). We find comparatively small differences in the salience of soil factors being
550 between -0.011 and 0.0156 (Supplementary Figure 3 C).

551 In general, the salience map of the weather and management data features fewer
552 broadly salient timepoints when interactions are included (Figure 3 A) than when they are not

553 (Figure 3 B). The weather and management CO model contains a broadly salient time point
554 around 25 days before planting and 6 days after planting. The SO model also appears to have
555 peaks of salience around 150, 183, and 199 days after planting. When interactions are included
556 the majority of the salient time points become less so with the exception of the peak 6 days after
557 planting as highlighted through subtraction of the two salience maps (Figure 3 C).

558

559 Discussion

560 Assumptions, Potential Sources of Error, and Opportunities for 561 Improvement

562 The results of this study are best understood with the data used and assumptions made
563 kept in mind. The sole source of biological data in this study came from the Genomes to Fields
564 Initiative (McFarland *et al.* 2020). The scale of this ambitious project increases the chances of
565 data being absent or compromised due to equipment malfunction, logistical or procedural
566 issues, and resource constraints. For example, many sites lack measurements for many soil
567 properties across the seasons considered here, and the timing of fertilizer applications was
568 absent in some cases. Our aim was to minimally filter the dataset while preventing missing or
569 distorted values (many of which are not missing at random) from altering model accuracy and
570 feature salience. We have aimed to reproducibly infer missing or aberrant values with relatively
571 simple methods (e.g., imputation using linear models, KNN, etc.) but more sophisticated
572 imputation techniques may have improved performance.

573 Alternatively, constraining the dataset to reduce the required imputation may have been
574 an effective strategy. We elected to minimally filter observations because machine learning
575 models, particularly deep learning, often benefit from having an abundance of data from which

576 to learn feature relationships. For models where this is not the case, restriction of observations
577 to the observations with the highest quality may be a preferable strategy. Note, however, that for
578 distortions that are not randomly distributed, filtering may bias the sample and result in a model
579 that appears to perform well but generalizes poorly (e.g., to sites similar to those with a
580 preponderance of observations excluded).

581 Beyond including as many distinct locations and seasons as we could, we approximately
582 balanced site by year groups through down sampling to avoid overfitting our DNNs to sites with
583 more observations or biasing the selection of hyperparameters. This reduces the size of the
584 dataset that can be used in training. Although outside the scope of this study, assessment of the
585 sensitivity of DNNs to unbalanced group sizes, or exploration of alternate means of balancing
586 groups (e.g., randomly *up sampling* small groups to equal the size of larger groups) would be
587 valuable. Indeed, if balance were not a concern, or if it could be effectively achieved without
588 discarding observations in some groups, one could potentially employ more strict data filtering
589 without producing a dataset too small to benefit from machine learning.

590 Substantial effort was devoted to producing testing, training, and validation sets that
591 would not lead to overconfidence in the accuracy of our models. To this end we kept
592 observations within site-by-year groups in the same partition of the data. In effect, this prevents
593 the model from being trained and tested on the same weather and management data.
594 Furthermore, except in cases where soil features are static from season to season, the model
595 will not be trained and tested on observations with identical soil features. Proceeding in this
596 manner rather than selecting observations at random for the testing set further reduces an
597 already small number of weather and management conditions. Incorporating historical data
598 (Washburn *et al.* 2021) or expanding the dataset to include data from other sources represent
599 two possible avenues to incorporate a greater diversity of weather and management conditions
600 without compromising the testing set.

601 Depending on the intended application of a model, one may be able to achieve higher
602 performance through altering some of the above decisions or replacing random assignment with
603 a targeted approach. For example, we assume that all group-by-year combinations are equally
604 likely to be of interest. However, if we assume that the distribution of sites collected match those
605 of interest for prediction (i.e., one is interested in predicting *any* future observation collected by
606 G2F and the number of observations per field site are representative of future number of
607 observations) then down sampling can be skipped, resulting a larger dataset. Similarly, with a
608 narrower aim, e.g., prediction of yield within a specific region, testing or validation sets could be
609 constrained to better select hyperparameters for or assess predictive accuracy of site-by-year
610 combinations within that region.

611 In summary, our decision to include as much data as possible and to limit the possibility
612 of overfitting to specific sites and seasons represent possible opportunities for improvement.
613 More sophisticated data imputation or more restrictive filtering, alternate means of balancing
614 groups, and the incorporation of other data sources have the potential to improve model
615 performance. Additionally, for more narrowly purposed models, non-random testing and training
616 sets may represent a more accurate metric of predictive power, and indeed may deviate
617 substantially from what we show here.

618 Tradeoffs in Model Performance and Computational Resources

619 While the best performance was achieved with a deep neural network incorporating
620 genomic, soil, weather, and management data, simple linear models with fixed effects often
621 performed nearly as well (Figure 2). This is notable because tuning and training deep neural
622 networks requires significant computational resources and time. For example, hyperparameter
623 tuning in the machine learning models shown here took less than 24 hours to complete whereas

624 tuning a single DNN sub-network took up several days. In the case of the best performing model
625 this was repeated four times – once for each sub model.

626 By contrast, linear models, particularly those with only fixed effects, are quick to fit. They
627 also outperformed many of the machine learning models, despite not undergoing extensive
628 tuning for model structure. In cases where accuracy is not the sole factor under consideration,
629 or where time or computational resources are limiting, simpler models may be “good enough”
630 for the desired purpose.

631 Usefulness of Consecutive Optimization in Hyperparameter 632 Selection

633 We employed two strategies for hyperparameter optimization: consecutively optimizing
634 (CO) hyperparameters for distinct “modules” of the network and simultaneously optimizing (SO)
635 the network as a whole. CO reduces the range of possible combinations that are explored by
636 allowing only one module to vary at a time. However, if two features in different data sets have a
637 strong interaction effect (e.g., between genotype and weather patterns) then this approach will
638 not necessarily allow for optimization to better capture this interaction. SO represents the
639 reverse situation. With all features available, interactions between features in different tensors
640 can be leveraged, but the hyperparameter space to explore is larger as all the hyperparameters
641 are free to vary.

642 We find that the network resulting from CO substantially outperforms the one generated
643 through SO. This should not be taken as a problem with SO *per se*. In other applications, or with
644 a different optimization algorithm, it may prove to be a more efficient means of deriving a useful
645 architecture. Furthermore, it is conceivable that SO is effective but that additional trials were
646 required. The SO DNN architecture was selected based on 40 trials whereas the CO DNN
647 architecture was selected based on 40 trials *for each module* (160 trials across the whole

648 network) which confounds comparison. Selection of the training duration also warrants
649 consideration. The SO model is capable of performing comparably to the CO model, but overfits
650 more rapidly (Figure 1 B). Improved heuristics for selecting the training duration could increase
651 usefulness of the SO model while reducing computational demands as well.

652 As a pragmatic matter, CO benefits from the capacity to tuning multiple modules at once.
653 In our hands, total time spent tuning was driven more by modules with computationally intensive
654 components (e.g. convolution layers) rather than the number of modules to optimize. This
655 benefit is dependent on the tuning algorithm used. We used a bayesian optimization procedure
656 which aims to produce useful hyperparameter combinations in fewer cycles than a simpler
657 method such as grid approximation. However, because this method uses the performance of
658 previously evaluated hyperparameters in selecting the next set, it does not permit parallelization
659 in tuning a single network. If an optimization procedure that is conducive to parallelization were
660 used (e.g., Hyperband or grid approximation) with enough computational resources this benefit
661 would be non-existent.

662 Although we aimed to broaden the range of possible architectures relative to previous
663 modeling on G2F data (Washburn *et al.* 2021), we constrained the overall structure to
664 processing each tensor individually then allowing for interactions between the final layer of each
665 module. Other options might include, for example, allowing an interaction module use both the
666 first and final layers as input (instead of only the final one), or allow which layers were to be
667 used to be tuned.

668 An additional option that we did not explore is aiming to inform the structure of the
669 selected network based on known relationships between features. Similar to our decision to
670 minimally transform and filter the data, we elected to avoid “nudging” the architecture of the
671 network in any direction in order to allow the data to inform it instead. Informing the model

672 architecture based on known relationships, analogous to incorporating a prior, remains an
673 interesting and potentially fruitful avenue to pursue.

674 Feature Importance

675 Similar to the results of previous modeling (Washburn *et al.* 2021), we find that no single
676 data grouping provides sufficient information to disregard all others. We note that weather and
677 management data does reduce error substantially relative to genetic and soil data, but the
678 variation in performance is large (Figure 2). Only after integration of all data types do we see a
679 relative reduction in error and consistency in this reduction.

680 Here we focus on salience in the weather and management data as it provided the best
681 average performance when used without other datasets. We find that the total water applied to
682 the field (including irrigation and rainfall, termed “WaterTotalInmm”) is the most influential factor
683 for determining yield (Figure 3, Supplementary Figure 3 D). This is sensible from a biological
684 standpoint and is in agreement with previous models. Previous DNNs developed with a subset
685 of G2F data also identified precipitation as substantially influencing yield (Washburn *et al.*
686 2021). Linear modeling results find similar results and suggest a positive association between
687 precipitation early in development and yield (Rogers *et al.* 2021). Additionally, in a recent study
688 using a hybrid machine learning and crop growth model prediction system, the authors found
689 that water related features (e.g. average drought stress, average water table in season) were
690 important, although not as important as the trend in genetic and management improvements
691 over time (Shahhosseini *et al.* 2021). The daily average of solar radiation
692 (“SolarRadiationMean”) is the next most salient feature of this dataset, followed by the
693 maximum temperature (“TempMax”) and the average wind direction (“WindDirectionMean”). A
694 study employing a convolutional recurrent DNN to model county level data likewise found solar
695 radiation and maximum temperature as important features and note an apparent increase in the

696 importance of temperature near planting time (Khaki *et al.* 2020). A time dependent sensitivity
697 can be observed in our model as well (Figure 3).

698 The relationship driving the high average salience of the average wind direction is not
699 clear. This feature likely correlates with unrecorded variables. Assessment of the topology and
700 geographical surroundings of each field site to suggest what this measure may be linked to lies
701 outside the scope of this study.

702 With respect to management interventions, although addition of N, P, or K are not
703 among the most salient weather and management features, we observe that nitrogen does have
704 a mean salience comparable to relative humidity and photoperiod, while phosphorus and
705 potassium are far lower. As noted in previously (Washburn *et al.* 2021) limited salience of
706 fertilizers could be due to the quantities used being too low to exert a substantial effect, or
707 alternatively application of these elements may be insufficiently variable to reveal the effect.

708 Importance of GEM Interactions Accuracy in Feature Salience

709 Incorporating interactions between genetic, environmental, and management factors
710 appears to have benefitted the accuracy of the resultant models. The CO DNN with interactions
711 performed best (nRMSE 14.554%, RMSE 0.948) with the next best models, CO weather model
712 and SO Models performing comparably (nRMSE 15.715%, RMSE 1.024). However, the two
713 DNNs with interactions have far lower dispersion in RMSE, with standard deviations of 0.013 in
714 the CO model and 0.035 in the SO model as compared with 0.074 in the CO weather model.

715 Interactions not only improve accuracy and model consistency across replicates, there
716 appear to be changes in the salience of individual features as well. This is most apparent in
717 considering weather and management features' salience (Figure 3 C). Relative to the sub
718 model, incorporating interactions appears to increase the salience of irrigation, although it is
719 highly salient in both models (relative to other time series factors). Additionally, several broadly

720 salient points in time, two of which are at the extreme end of the season, have diminished
721 salience with the incorporation of interactions. This reduction is not uniform across all highly
722 salient time points. A strong peak in salience shortly after planting is seen in both saliency maps
723 which agrees with previously reported results (Washburn *et al.* 2021).

724 Conclusions and Future Directions

725 The consecutively optimized deep neural network model developed here shows promise
726 for complementing existing models for crop selection and improvement, as it produces more
727 accurate estimates of yield than the other considered models. Of particular interest here is the
728 capacity of this and other convolutional neural networks to incorporate change in environmental
729 variables over time. This enables the generation of counterfactuals to examine the expected
730 effect of different planting times (shifting the planting date of a site relative to the true value),
731 planting in different sites, or planting under future possible climate scenarios. Additionally, the
732 ability to generate such estimates would enable breeders to consider not only the expected yield
733 of an individual cultivar but the expected *consistency* of yield as well.

734 For such a strategy to be adopted in genomic selection, further efforts are needed to
735 validate the predictions such a model produces. This will necessitate incorporating of and
736 validation on future data from the Genomes to Field Initiative (McFarland *et al.* 2020) or other
737 large-scale experiments. The Genomes to Field Initiative and other organizations sponsor
738 prediction competitions and other activities designed to advance this area of study.
739 Furthermore, applying the same model or the approach used to develop it to other crops would
740 be a valuable step towards assessing its' broad scale usefulness. This would also potentially
741 implicate groups of crops for which the same model may be used through transfer learning,
742 along with groups that require crop-specific models to be developed.

743 Additional improvements to accuracy that have the potential to transfer to modeling
744 efforts for other crops include improved heuristics for epoch selection and training set
745 construction. The simultaneously optimized model achieves a minimum error *lower* than our
746 selected model (see Figure 2) and does so in far fewer epochs, but overfits much faster as well.
747 If overfitting were preventable through a better heuristic for epoch selection than the one we
748 employed, simultaneous optimization would have produced a better performing model that was
749 simpler to generate. Training set construction is another opportunity for improvement with
750 transferable utility. Here we took an aggressive approach ensuring approximately balanced
751 groups, down sampling all groups with observations in excess of the smallest group in the test
752 set. Deep neural networks tend to perform better with an abundance of data, so alternate
753 approaches that retain more observations are of interest. In cases where there are few
754 observations or model development is heavily constrained by computational resources or model
755 development time, other models, especially linear regression models, may result in a model that
756 performs nearly as well as a deep neural network.

757 Deep learning models do not result in parameters which are as readily interpretable as
758 those of more standard statistical procedures and do not incorporate the physiology of the plant
759 as mechanistic crop growth models do. These represent ongoing challenges and limit the
760 scenarios in which a deep neural network may be useful. This can be partially addressed
761 through how the data is represented (e.g. using non-PC transformed data), which has been
762 explored for identification of genetic loci (Liu *et al.* 2019). Additionally, efforts to incorporate
763 known relationships into a deep learning model's structure have the potential to benefit
764 accuracy and interpretability. Improvements in the capacity to represent genetic or physiological
765 principles could allow for these methods to apply to a wider range of uses and address a
766 broader set of questions.

767

|

768 Author Contributions

769 Genomes to Fields experiments were coordinated and designed by Natalia DeLeon, David Ertl,
770 Judith Kolkman, Dayane Cristina Lima, Danilo Moreta, James Schnable, and Maninder Singh.
771 Field experiments were conducted, and data was collected and curated by Barış Alaca, Tim
772 Bessinger, Natalia DeLeon, David Ertl, Sherry Flint-Garcia, Candice Hirsch, Joseph Knoll,
773 Judith Kolkman, Dayane Cristina Lima, Danilo Moreta, James Schnable, Maninder Singh, Jason
774 Wallace, Jacob Washburn, and Teclé Weldekidan. Joseph Gage provided novel genomic data.
775 David Ertl and Maninder Singh contributed funding to the Genomes to Fields Initiative.
776
777 The computational study was designed by Daniel Kick and Jacob Washburn. Additional data
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781

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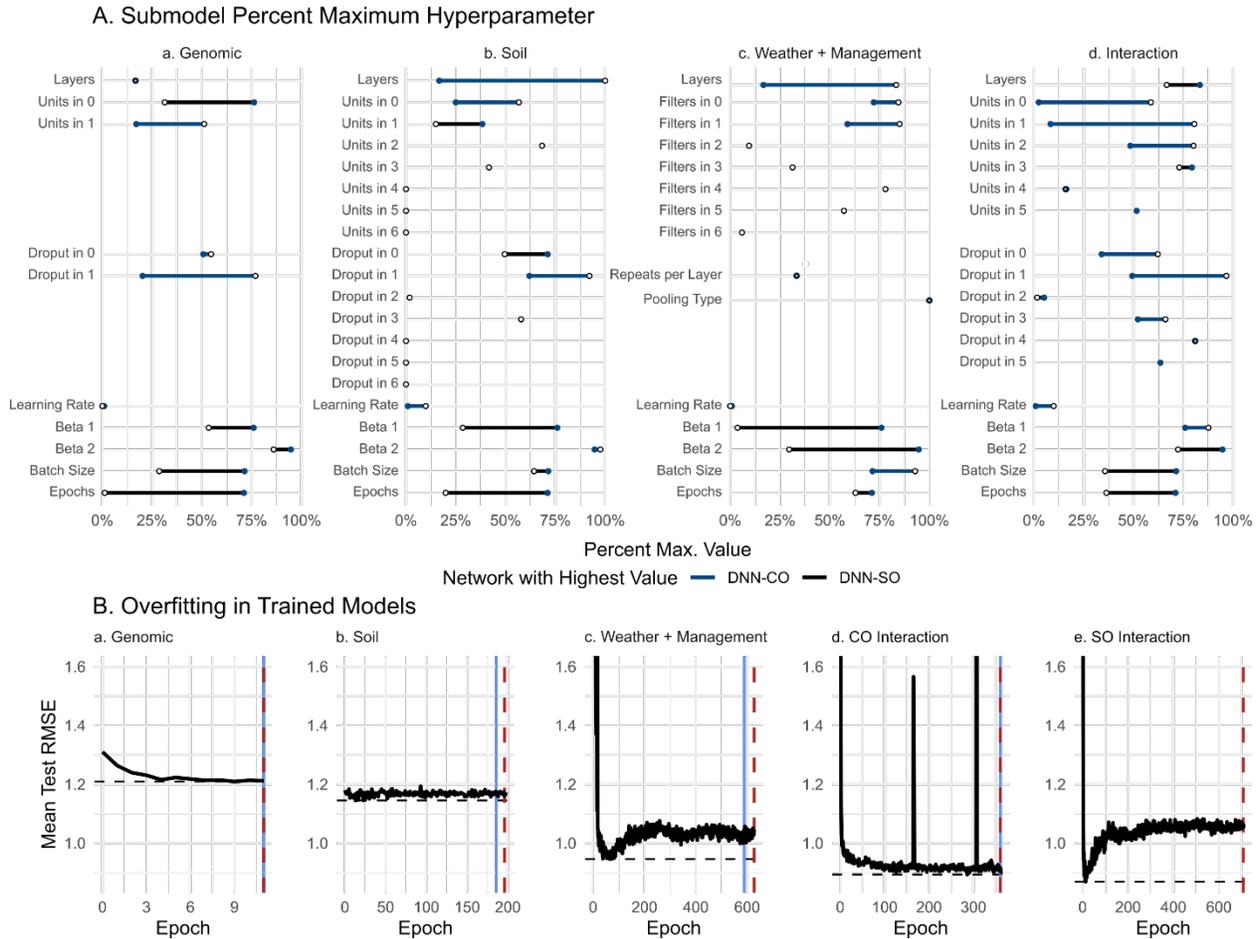
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917 Figures

918 Figure 1. Optimization strategy results in different network
 919 architectures and degree of overfitting in full model

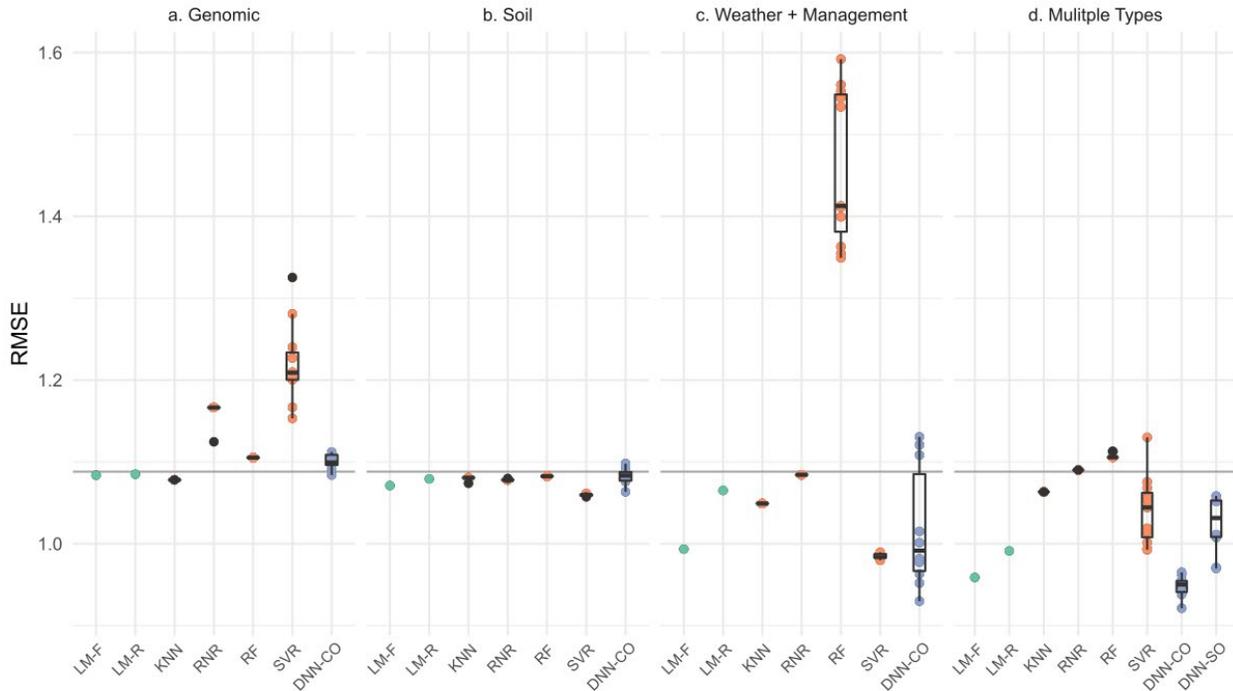


920
 921 **A.** Hyperparameters for each optimization strategy are shown as a percent of the allowed
 922 range. Data available for training is the same but the Consecutive Optimization (CO) and
 923 Simultaneous Optimization (SO) strategy result in substantially different hyperparameter values
 924 and thus network architecture. For exact values refer to Table 2 and Table 3. **B.** The average
 925 RMSE of the test set (across 10 replicates to account for random initialization of weights) is
 926 shown in black for each submodel (**a. – e.**). The horizontal dashed black line indicates the
 927 minimum error achieved throughout the training duration. The vertical lines indicate the
 928 difference in error and epochs of the minimum value and the values selected through minimizing

929 total validation error (red dashed line), the heuristic used in this study, and the mean plus
930 standard deviation of validation error (solid blue line), which was considered but not used. Both
931 strategies considered failed to select the epoch resulting in the minimum loss in the test set for
932 all submodels and resulted in apparent overfitting in the Weather and Management submodel
933 (c.) and the SO model (e.). For additional comparisons of heuristic performance see Table 4.
934

935 Figure 2. Model Performance Across Methodologies and Data 936 Types

A. Performance on Test Set in Root Mean Squared Error

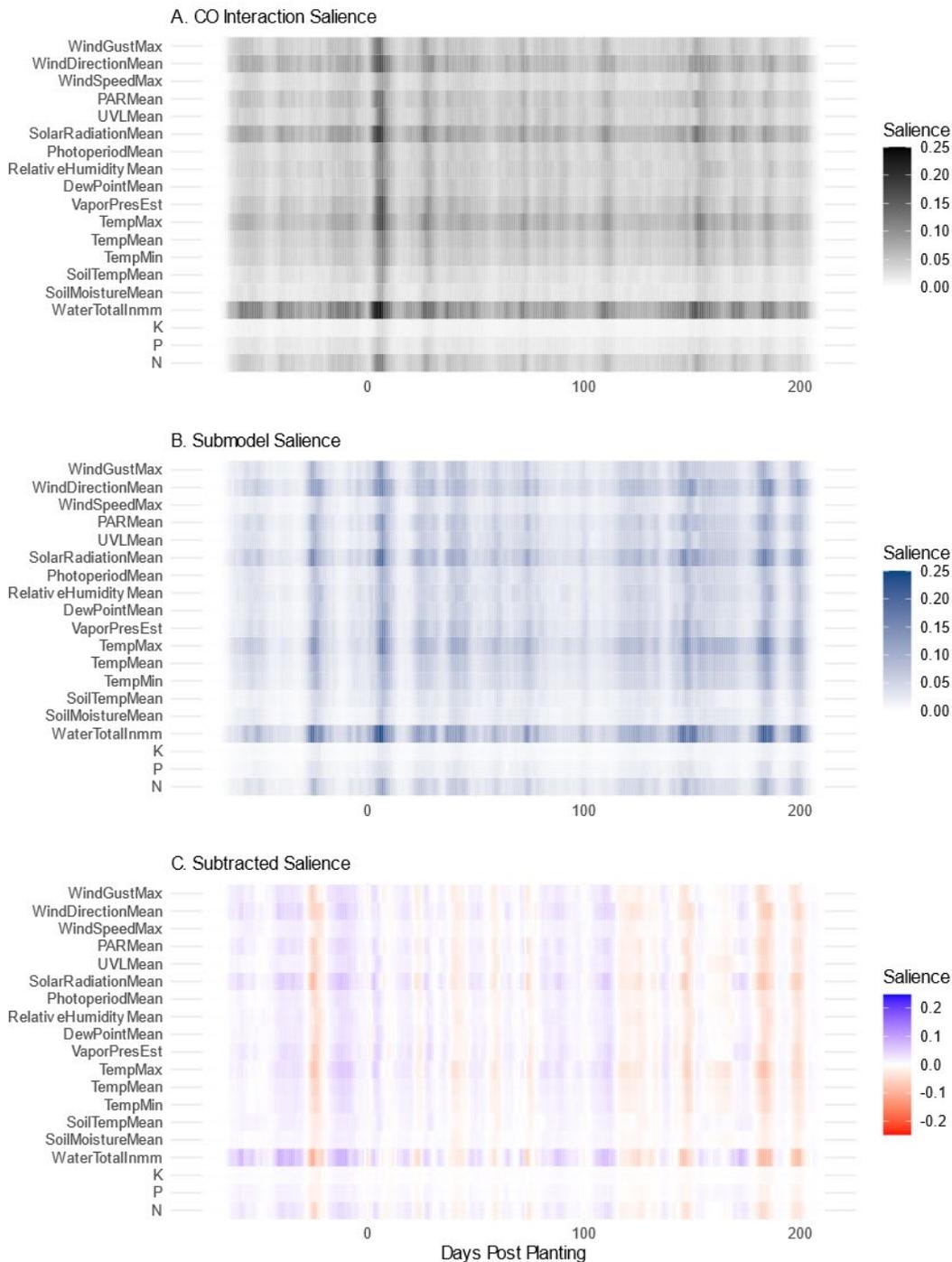


937
938 **A.** The root mean squared error (RMSE) of the testing set is shown for each data grouping
939 (panels a - d) and class of model. Lower values indicate better model performance. The
940 horizontal gray line indicates the performance of an intercept model, i.e. using the mean of the
941 training set yield as the prediction for all observations in the test set. For models that depend on
942 a seed value the RMSE values for ten trials (evaluated on the same data) are shown and
943 standard Tukey box plots are provided. In deep learning models random initialization of weights
944 at the beginning of training result in different performance across trials. Three groups of models
945 are shown, linear models (green), machine learning models (orange), and deep learning models
946 (blue). Linear models are subdivided into those with exclusively fixed effects (LM-F) and those
947 with random effects (LM-R). The best performing linear model is shown. For LM-F and LM-R
948 respectively these are utilizing the first 8 PCs (explaining 31% of the variance) in **a**, utilizing all
949 soil variables (for both LM-F and LM-R) in **b**, utilizing the five most salient weather/management

950 factors (for both LM-F and LM-R) in **c**, and the first 8 genomic PCs, 5 most salient
951 weather/management variables, and interactions between the two (for both LM-F and LM-R) **d**.
952 Machine learning models used were K-Nearest Neighbors (KNN), Radius Neighbor Regression
953 (RNR), Random Forest (RF), and Support Vector Regression with a linear kernel (SVR). Deep
954 learning models are divided by whether they were part of the Consecutive optimization strategy
955 (DNN-CO) or the Simultaneous optimization strategy (DNN-SO). Note that DNN-SO requires all
956 data types and thus only appears in panel **d**.
957

958 **Figure 3. Influence of Interaction Effects on Feature Saliency**

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960

961 **A.** Average saliency across all weather and management factors for each day considered.

962 Interaction model values shown in black. **B.** The same values in **A.** are shown for the submodel

963 in blue. Saliency peaks shortly after planting in both models. The submodel contains additional

964 peaks of salience prior to planting and near the end of the considered date range. **C.** Subtracted
965 salience values for the interaction model and the submodel. The interaction-containing model
966 appears to contain greater importance generally for certain features, e.g. irrigation and rainfall,
967 represented as “WaterTotalInmm”. The difference between the two saliency maps indicates
968 additional times of sensitivity in the submodel (approximately -25, +180, +195) that the
969 interaction model is relatively insensitive to.

970 Tables

971 Table 1. Hyperparameter Ranges: Deep Learning

Category	Submodels	Hyperparameter	Range	
Architecture	Genomic Only	Layers	1-7	
		Units	4-256	
		Dropout Fraction	0-0.3	
	Soil Only	Layers	1-7	
		Units	4-64	
		Dropout Fraction	0-0.3	
	Weather Only	Pooling Type	Max (1d), Ave. (1d)	
			Layer Repeats	1-7
		Convolution Layers per Repeat	1-4	
Filter Size			4 - 512	
Interactions		Layers	1-7	
		Units	4 - 256	
	Dropout Fraction	0-0.3		
Training	Optimizer	Learning Rate	0.1, 0.01, 0.001, 0.0001	
		Beta 1	0.9 - 0.9999	
		Beta 2	0.9 - 0.9999	
	Other	Batch size	32-256, step=16	
		Epoch	1-1000	

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974 **Table 2. Selected Deep Learning Hyperparameters: Architecture**

Submodel or Network	Hyperparameter	Specific Layer	Consecutive Optimization	Sequential Optimization
Genomic Only	Units	1	83	196
		2	133	47
	Dropout Fraction	1	0.163923177	0.15214
		2	0.230663142	0.06061
Soil Only	Units	1	38	19
		2	13	27
		3	45	
		4	29	
		5	4	
		6	4	
		7	4	
	Dropout	1	0.148724301	0.21342
		2	0.276340999	0.18589
		3	0.005434164	
		4	0.173380695	
		5	0	
		6	0	
		7	0	
Weather + Management Only	Pooling Type	N/A	Max	Max
	Convolution Layers per Repeat	N/A	2	2
	Filter Size	1	433	370
		2	436	303
		3	52	
		4	163	
		5	400	
6	294			
Interaction	Units	1	152	10
		2	207	25
		3	206	126
		4	188	204
		5	44	45
		6		134
	Dropout	1	0.18658661	0.10201
		2	0.289893588	0.14809
		3	0.004841293	0.01536
		4	0.198121953	0.15658
		5	0.243027717	0.2428
		6		0.19048

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977 **Table 3. Selected Deep Learning Hyperparameters: Training**

	Optimizer			Other	
Network	learning_rate	beta1	beta2	numEpoch	batch_size
CO: Genomic Only	0.0001	0.953368	0.985947	12	96
CO: Soil Only	0.01	0.928472	0.997516	199	176
CO: Weather Only	0.0001	0.903649	0.929582	629	240
CO: Full Network	0.01	0.98752	0.972311	364	112
SO	0.001	0.975893	0.994607	711	192

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979

980 **Table 4. Epoch Selection Underperformance**

Network	Epoch Selection By:			Average Test Loss:			Proportion of Minimum Loss		
	Mean + Standard Dev.	Best Epoch	Sum of Losses	Mean + Standard Dev.	Best Epoch	Sum of Losses	Mean + Standard Dev.	Best Epoch	Sum of Losses
CO: Genomic Only	10	10	12	1.209216	1.209216	1.21171	1	1.002063	0.002063
CO: Soil Only	161	14	199	1.178308	1.144793	1.172763	1.029276	1.024432	-0.00484
CO: Weather Only	225	66	629	1.041072	0.945608	1.046358	1.100955	1.106545	0.00559
CO: Full Network	362	287	364	0.912883	0.893123	0.903884	1.022124	1.012048	-0.01008
SO	796	14	711	N/A	0.86811	1.052109	N/A	1.211954	N/A

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983 **Table 5. Machine Learning Hyperparameter Optimization**

Model	Hyperparameter	Range	Genomic Only	Soil Only	Weather + Management Only	Multiple
KNN	Weight Metric	Uniform, Distance	Uniform	Distance	Uniform	Distance
	k	1 - 250	237	248	248	49
RNR	Weight Metric	Uniform, Distance	Distance	Distance	Uniform	Distance
	Radius	0.01 - 2000	39.759518	3.406197	5.986679	40.375418
SVR	Loss	Epsilon Insensitive, Squared Epsilon Insensitive	Epsilon Insensitive	Epsilon Insensitive	Epsilon Insensitive	Squared Epsilon Insensitive
	C	1 - 5 (log uniform)	2.772318	5.613996	4.623351	2.787589
RF	Max Depth	2 - 200, q = 1 (q uniform)	64	10	102	7
	Min Samples/Leaf	1 - 200, q = 1 (q uniform)	171	163	100	149

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986 **Table 6. Performance Across Data Sets**

Data Set	Model	mean RMSE	Standard Dev. RMSE	Mean nRMSE	Standard Dev. nRMSE	Mean R2	Standard Dev. R2
a. Genomic	DNN-CO	1.101	0.009	16.896%	0.142%	-0.117	0.019
	KNN	1.078	0.000	16.548%	0.000%	-0.072	0.000
	LM-F	1.084		16.635%		-0.083	
	LM-R	1.085		16.653%		-0.085	
	Mean	1.088		16.701%		-0.092	
	RF	1.105		16.965%		-0.126	
	RNR	1.163	0.013	17.846%	0.194%	-0.246	0.027
	SVR	1.219	0.049	18.718%	0.750%	-0.373	0.112
	b. Soil	DNN-CO	1.083	0.010	16.622%	0.152%	-0.081
KNN		1.080	0.002	16.578%	0.031%	-0.076	0.004
LM-F		1.071		16.441%		-0.058	
LM-R		1.079		16.566%		-0.074	
Mean		1.088		16.701%		-0.092	
RF		1.083		16.616%		-0.081	
RNR		1.078	0.001	16.549%	0.008%	-0.072	0.001
SVR		1.059	0.001	16.262%	0.017%	-0.035	0.002
c. Weather + Management		DNN-CO	1.018	0.074	15.627%	1.141%	0.040
	KNN	1.049		16.105%		-0.015	
	LM-F	0.993		15.249%		0.090	
	LM-R	1.065		16.349%		-0.046	
	Mean	1.088		16.701%		-0.092	
	RF	1.461	0.095	22.430%	1.455%	-0.977	0.256
	RNR	1.084		16.643%		-0.084	
	SVR	0.985	0.003	15.114%	0.050%	0.106	0.006
	d. Multiple Types	DNN-CO	0.948	0.013	14.553%	0.197%	0.171
DNN-SO		1.024	0.035	15.716%	0.531%	0.032	0.065
KNN		1.063	0.000	16.322%	0.000%	-0.043	0.000
LM-F		0.959		14.719%		0.152	
LM-R		0.991		15.217%		0.094	
Mean		1.088		16.701%		-0.092	
RF		1.107	0.003	16.991%	0.045%	-0.130	0.006
RNR		1.090	0.000	16.733%		-0.096	0.000
SVR		1.041	0.042	15.976%	0.643%	0.000	0.082

987